

PGLP: Customizable and Rigorous Location Privacy through Policy Graph

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Outline

- **Motivation**
 - why we need a customizable and rigorous location privacy model.
- **Our Solution: Policy Graph based Location Privacy (PGLP)**
 - a flexible interface for location privacy to tune privacy-utility tradeoffs.
- **PGLP for Location Trace Release**
 - challenges and countermeasures when using PGLP continuously.
- **Experiments**
- **Conclusion & Future work**

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Motivation

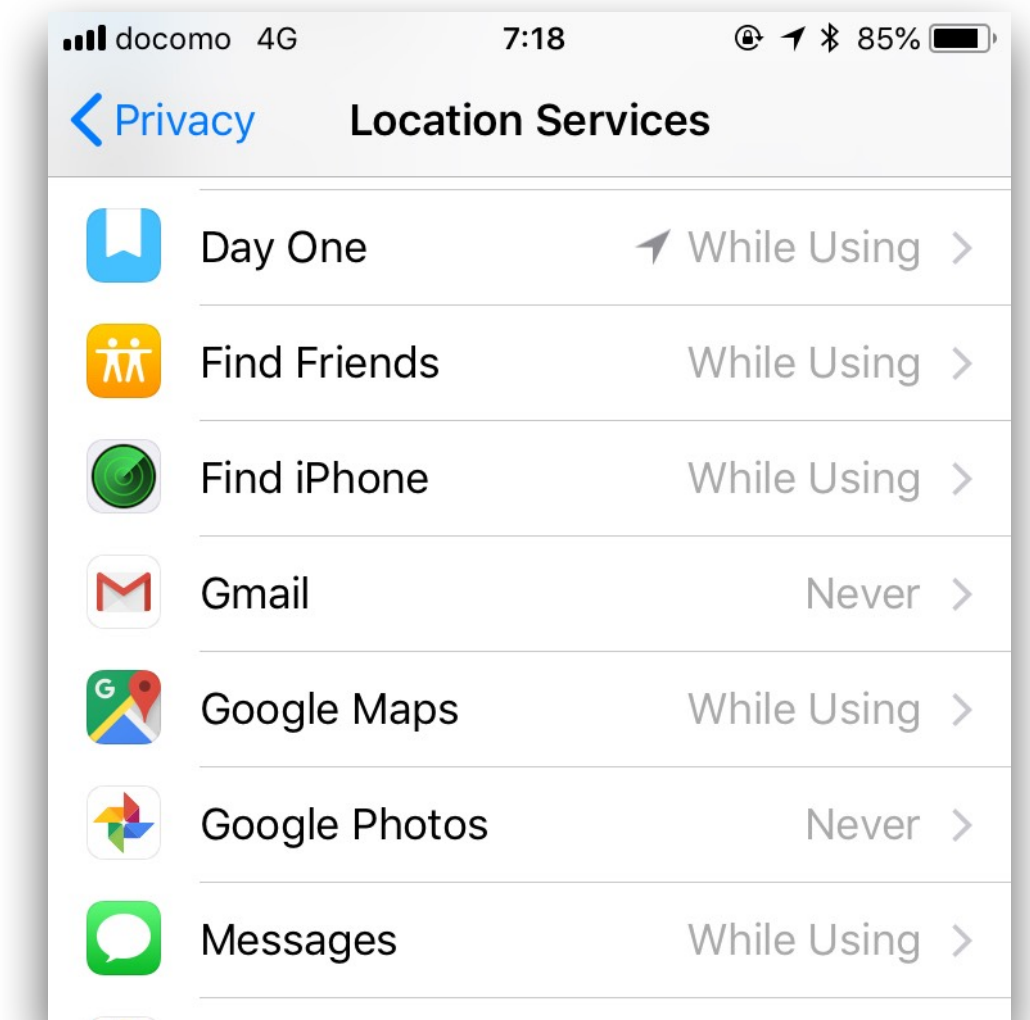
Location data: **valuable** but **sensitive**

- **Useful** in our daily life for Location-based Service (LBS)

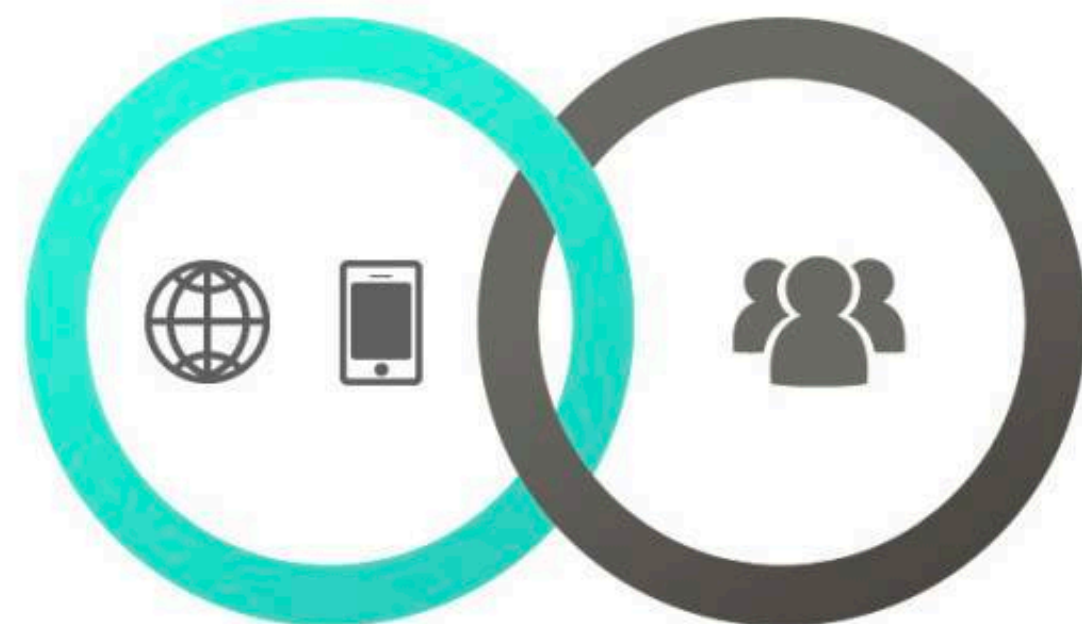


Uber

食ベログ



- **Fundamental** in research areas IoT, Crowdsourcing, Smart City..



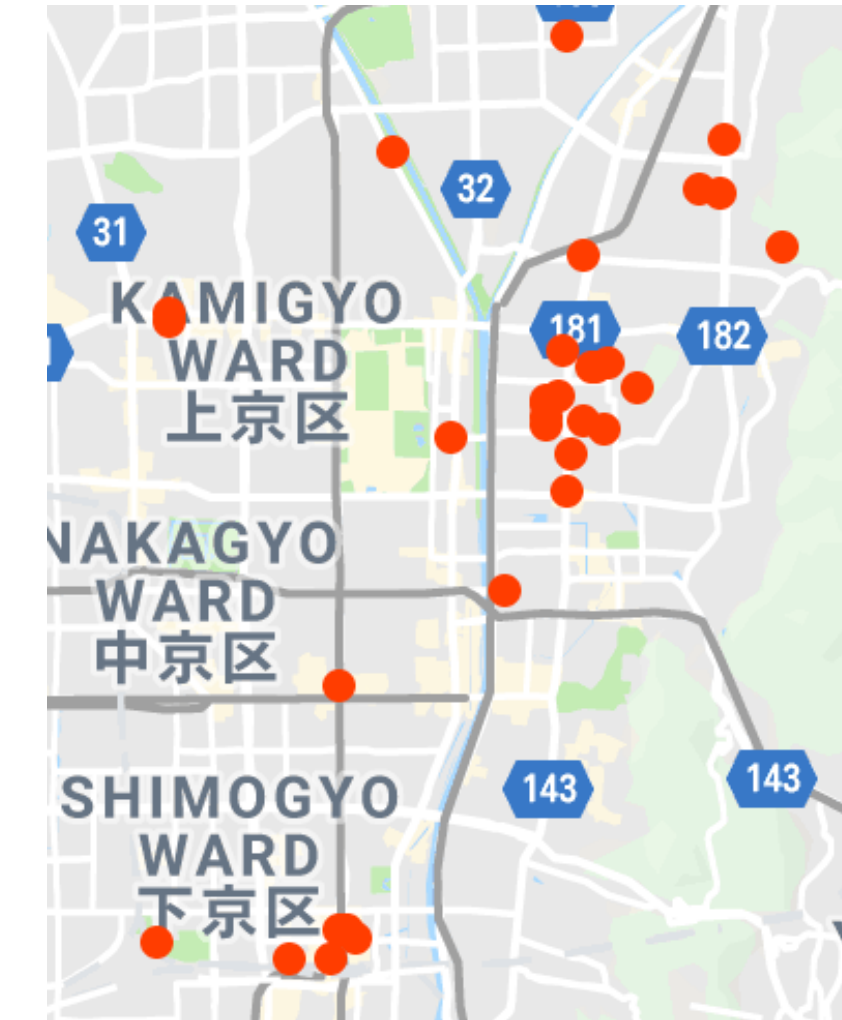
Online to Offline



Motivation

Location data: **valuable** but **sensitive**

- risky for an individual
 - ▶ reveal many sensitive info: **identification, home, office, lifestyle, hobbies...**



Google Map “frequently visited locations”

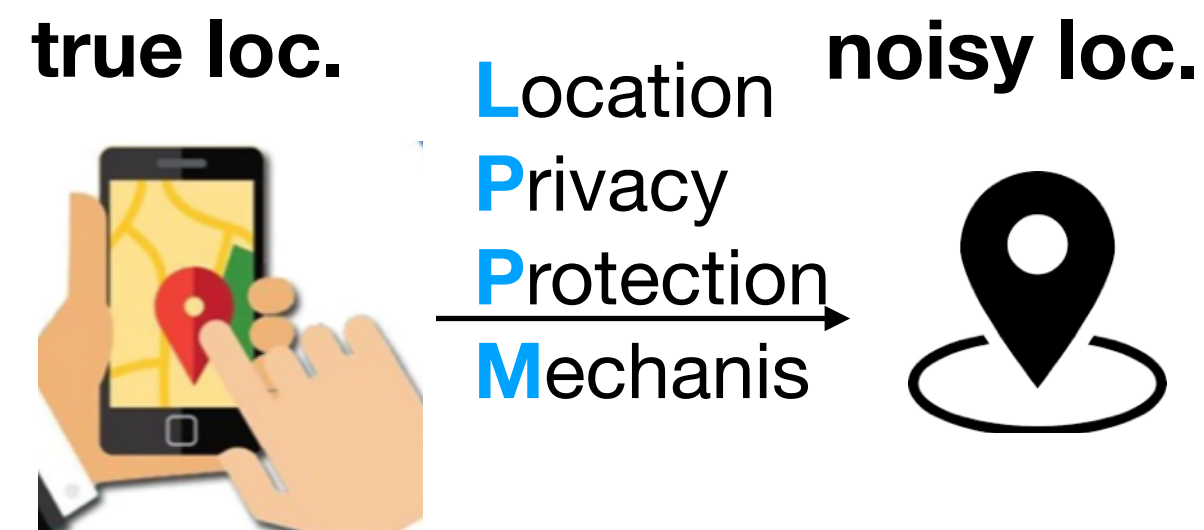
- risky for companies who utilize user location data



Motivation

How to Protect Location Privacy

- ▶ general **idea**: add **uncertainty** to the true location



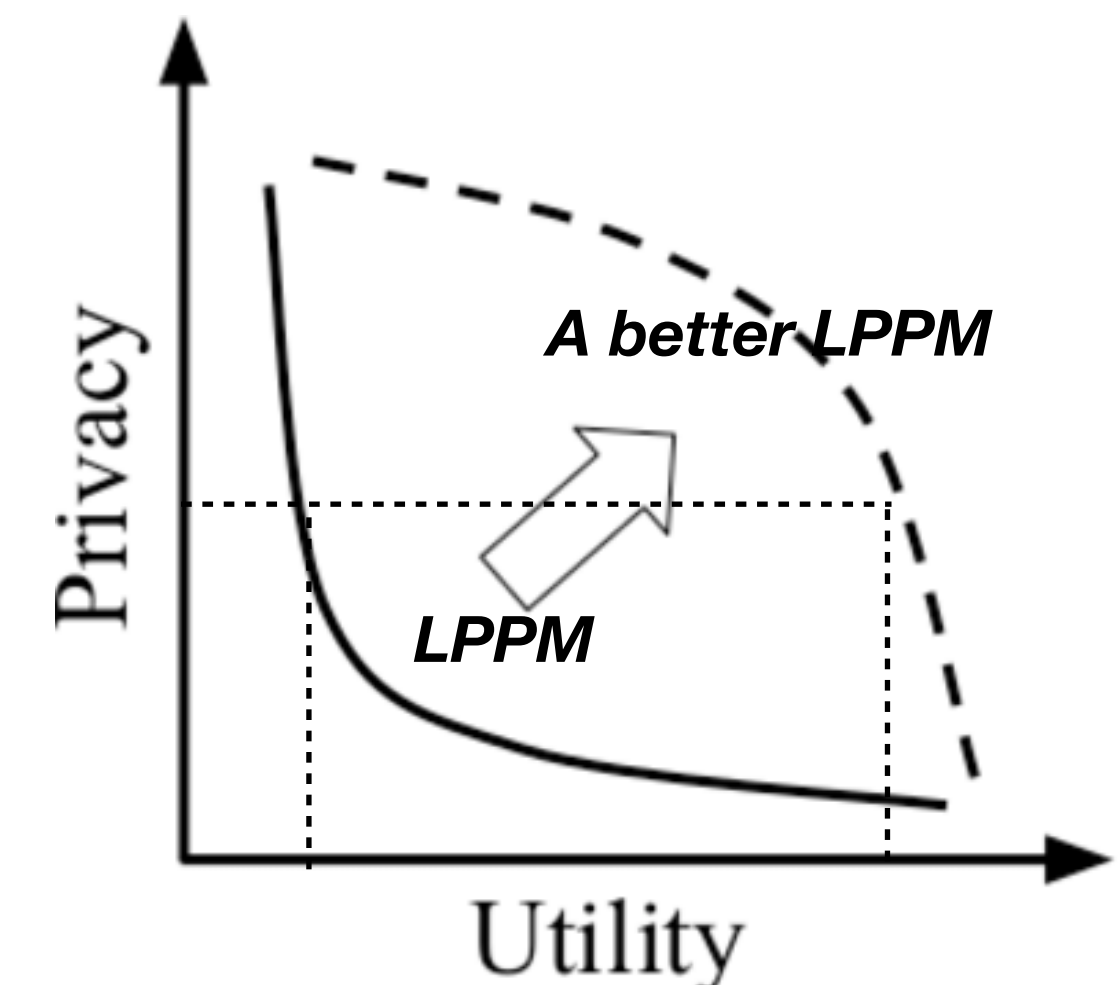
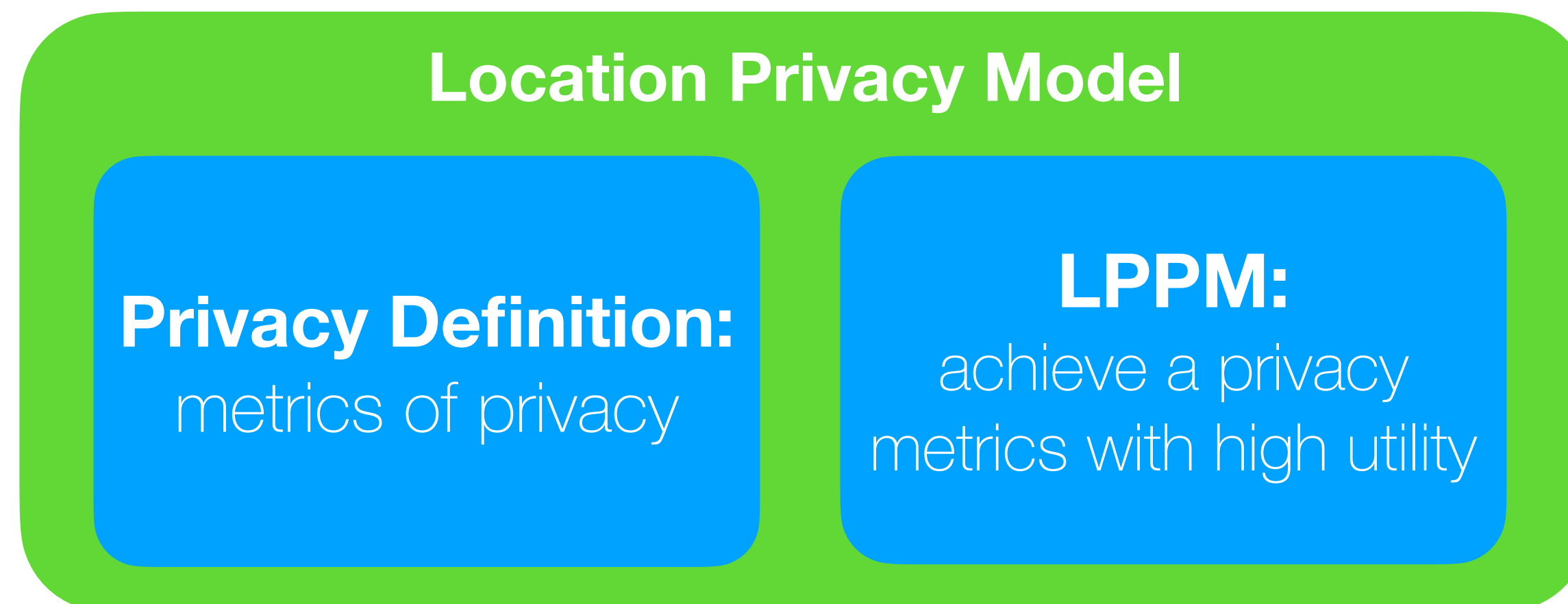
“what is weather tomorrow near my location?”



My location = *Kyoto University* better utility

My location = *Kyoto City.* better privacy

- ▶ general **research goal**: better tradeoff between **privacy** and **utility**



Motivation

Existing Location Privacy Definitions

extended from K-anonymity

- ▶ location k-anonymity, [MobiSys03].
- ▶ mix zone, [PerCom03].
- ▶ The New Casper [VLDB06].
- ▶ maximum arrival boundary [TKDE12].

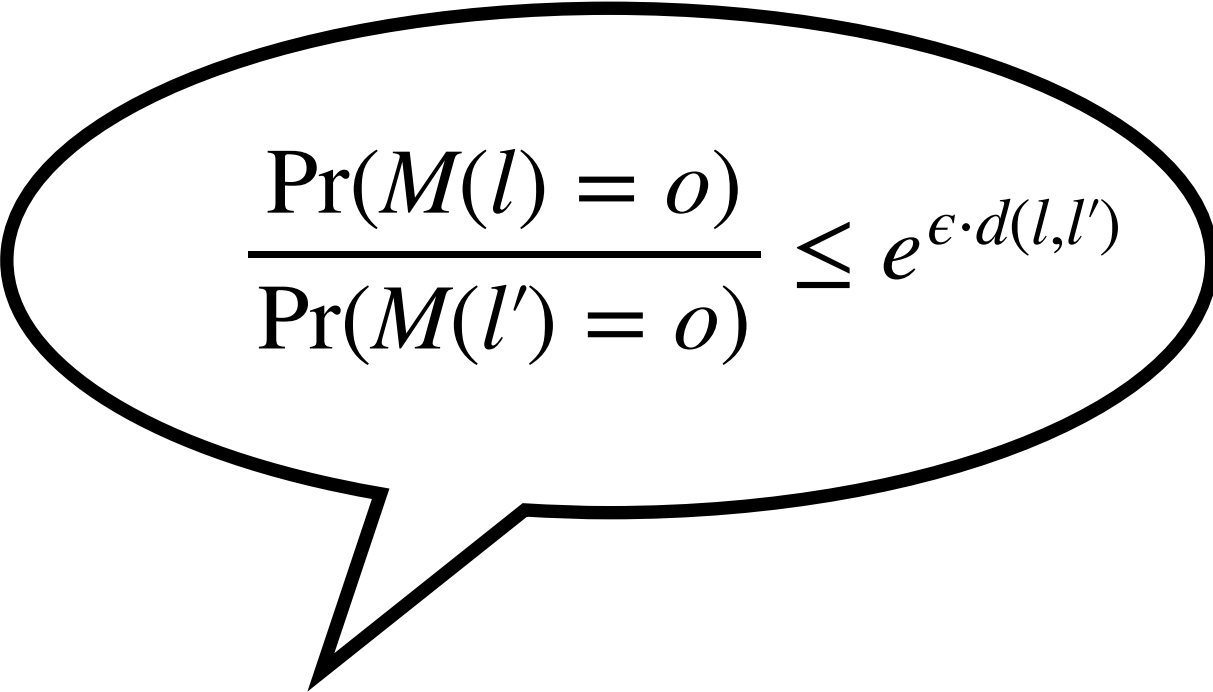
extended from Differential Privacy (DP)

- ▶ Geo-Indistinguishability [CCS13].
- ▶ δ -location set privacy [CCS15].

Motivation

Existing Location Privacy Definitions **are Not Sufficient**

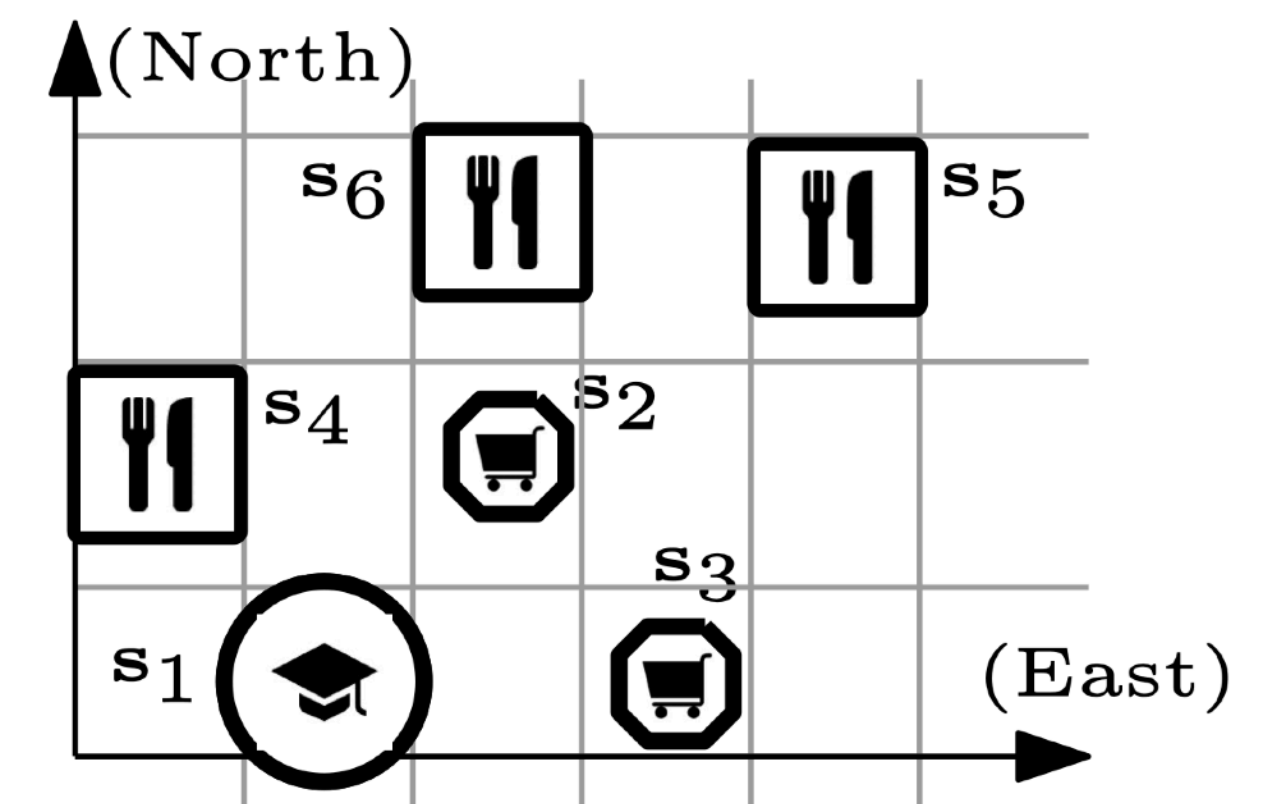
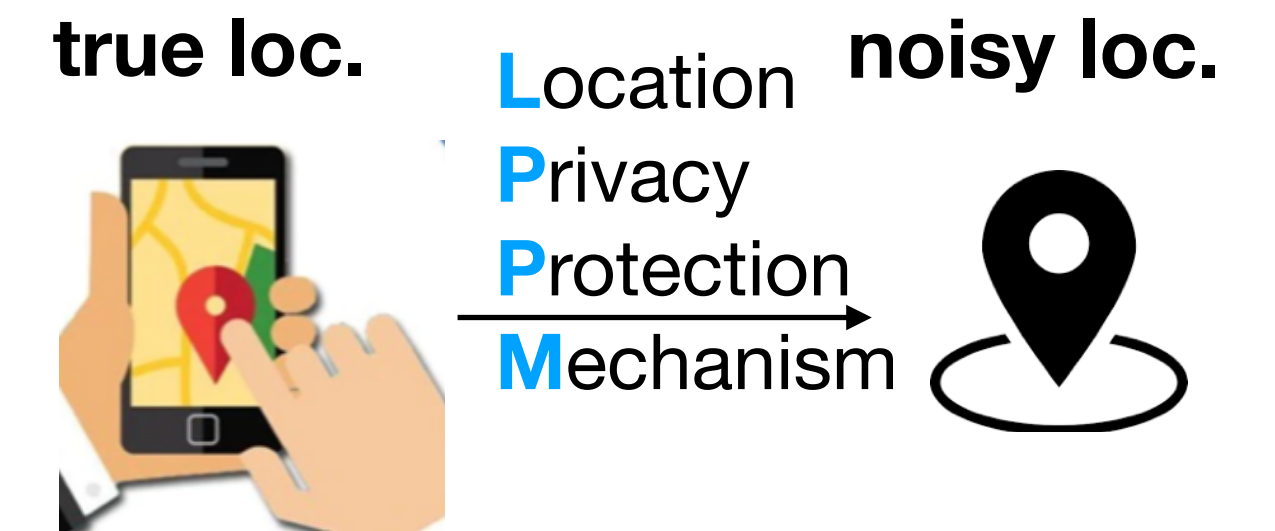
- K-anonymity based Location privacy is **not rigorous**
 - L-diversity argue K-anonymity has flaws
 - T-closeness say: L-diversity has flaws
 -
- Existing DP-based location privacy is **not customizable**
 - **Only use one parameter ϵ** to control the privacy-utility trade-off.
 - However, different LBS may have different requirements on privacy or utility.


$$\frac{\Pr(M(l) = o)}{\Pr(M(l') = o)} \leq e^{\epsilon \cdot d(l, l')}$$

Motivation

Different LBS, Different Utility Requirement

- City-level weather forecast
 - Query: which city is the user in?
 - High utility when the noisy location is in **the same city** of the true location.
- Location-based advertising
 - Query: what kind of loc. (shopping mall/restaurant) is the user in?
 - High utility when the noisy location has **the same category** of the true location.
- Location-based Social Network
 - Query: where is my nearest friend?
 - High utility when the **distance** between two noisy locations is similar to the distance between the true locations.



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Our Solution

Intuitions for a Customizable and Rigorous Location Privacy

- Inspired by Blowfish Privacy [SIGMOD14], the privacy-utility Tradeoff can be fine-tuned by “*Privacy Policies*”:
 - **secrets**: what are the secrets that we need to protect?
 - **constraints**: what does the adversary know?
- However, Blowfish Privacy cannot be directly applied in location privacy.
 - Location privacy: single user, point query on single record (location).
 - Statistical privacy: multiple users, aggregate query on a database.
- How to formalize [Location Privacy Policy](#) and how to achieve it?

Our Solution : PGLP

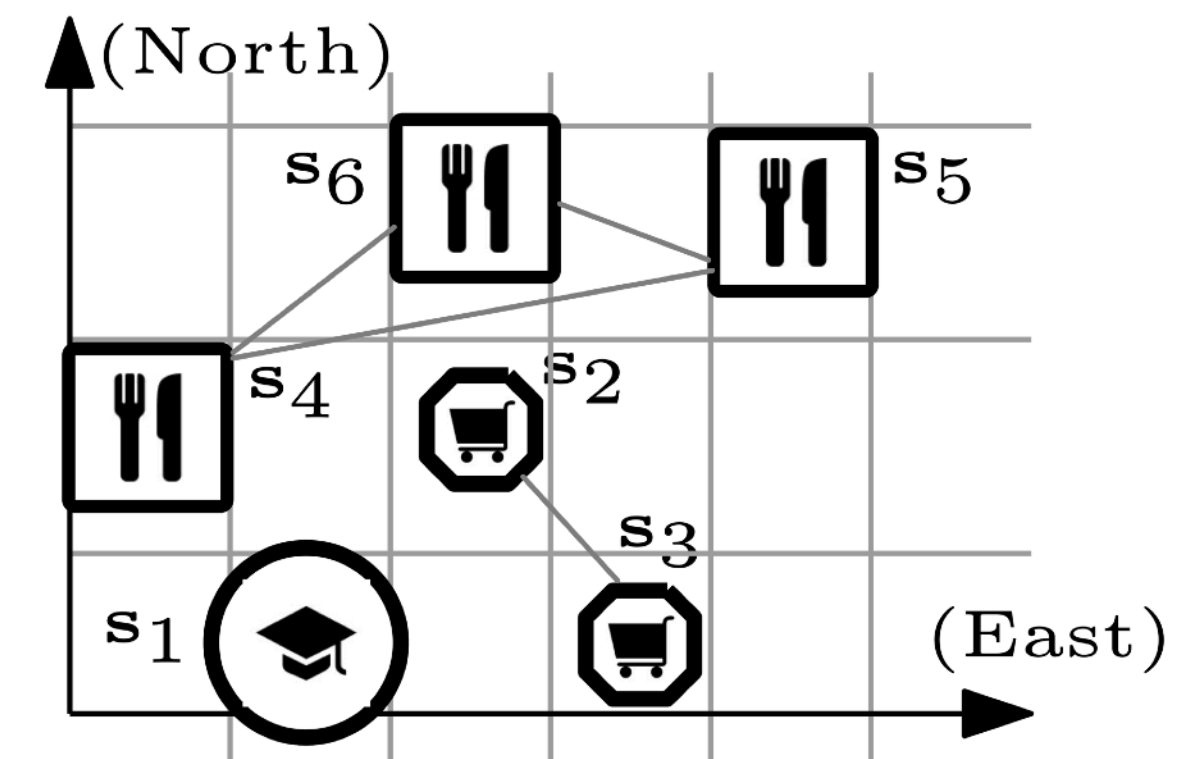
Location Policy Graphs

- How to formalize these policies? — [Location Privacy Policy Graph](#)

- **Nodes**: the user's possible locations.
- **Edges**: the two connected locations need to be indistinguishable to the adversary

- The right policy is a good fit for “Location-based advertising”

- High utility if the noisy location has the same category of the true location.
- Policy: “*allowing the app to access the semantic category (e.g., a restaurant or a shop) of a user's location but ensuring indistinguishability among locations with the same category*”



Our Solution : PGLP

Definition

- **key idea:** only satisfy the indistinguishability defined in the given policy graph.
- Location Policy Graph:

Definition 3 (Location Policy Graph). *A location policy graph is an undirected graph $\mathcal{G} = (\mathcal{S}, \mathcal{E})$ where \mathcal{S} denotes all the locations (nodes) and \mathcal{E} represents indistinguishability (edges) between these locations.*

- Policy Graph-based Location Privacy:

Definition 6 ($\{\epsilon, \mathcal{G}\}$ -Location Privacy). *A randomized algorithm \mathcal{A} satisfies $\{\epsilon, \mathcal{G}\}$ -location privacy iff for all $z \subseteq \text{Range}(\mathcal{A})$ and for all pairs of neighbors s and s' in \mathcal{G} , we have $\frac{\Pr(\mathcal{A}(s)=z)}{\Pr(\mathcal{A}(s')=z)} \leq e^\epsilon$.*

Our Solution : PGLP

Definition

- PGLP is a **generalization** of DP-based location privacy definitions.
- it reduces to Geo-Indistinguishability [CCS13] and δ -location set privacy [CCS15] under different configuration of the policy graph.

Theorem 1. *An algorithm satisfying $\{\epsilon, \mathcal{G}_1\}$ -location privacy also achieves ϵ -Geo-Indistinguishability.*

Theorem 2. *An algorithm satisfying $\{\epsilon, \mathcal{G}_2\}$ -location privacy also achieves δ -Location Set privacy.*

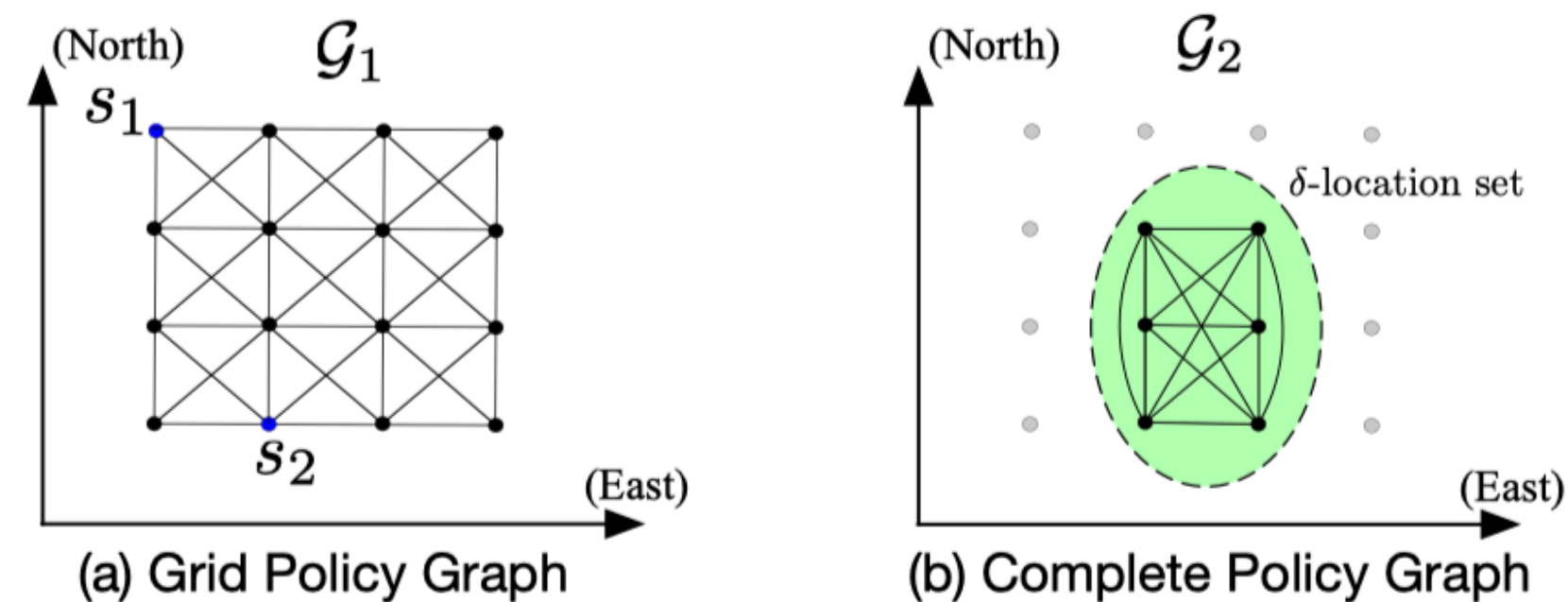


Fig. 2: Two examples of location policy graphs.

Our Solution : PGLP

Mechanisms

- **key idea:** calibrate the sensitivity w.r.t. a given policy graph.

Algorithm 1 Policy-based Laplace Mechanism (P-LM)

Require: ϵ , \mathcal{G} , the user's true location \mathbf{s} .

- 1: Calculate $S_f^{\mathcal{G}} = \sup \| (f(\mathbf{s}) - f(\mathbf{s}')) / d_{\mathcal{G}}(\mathbf{s}, \mathbf{s}') \|_1$ for all $\mathbf{s}' \in \mathcal{N}^{\infty}(\mathbf{s})$;
 - 2: Perturb location $\mathbf{z}' = f(\mathbf{s}) + [Lap(S_f^{\mathcal{G}}/\epsilon), Lap(S_f^{\mathcal{G}}/\epsilon)]^T$;
 - 3: **return** a location $\mathbf{z} \in \mathcal{S}$ that is closest to \mathbf{z}' on the map.
-

Algorithm 2 Policy-based Planar Isotropic Mechanism (P-PIM)

Require: ϵ , \mathcal{G} , the user's true location \mathbf{s} .

- 1: Calculate $K(\mathcal{G}) = Conv \| (f(\mathbf{s}) - f(\mathbf{s}')) / d_{\mathcal{G}}(\mathbf{s}, \mathbf{s}') \|_1$ for all $\mathbf{s}' \in \mathcal{N}^{\infty}(\mathbf{s})$;
 - 2: $\mathbf{z}' = f(\mathbf{s}) + Y$ where Y is two-dimension noise drawn by Eq.(1) with sensitivity hull $K(\mathcal{G})$;
 - 3: **return** a location $\mathbf{z} \in \mathcal{S}$ that is closest to \mathbf{z}' on the map.
-

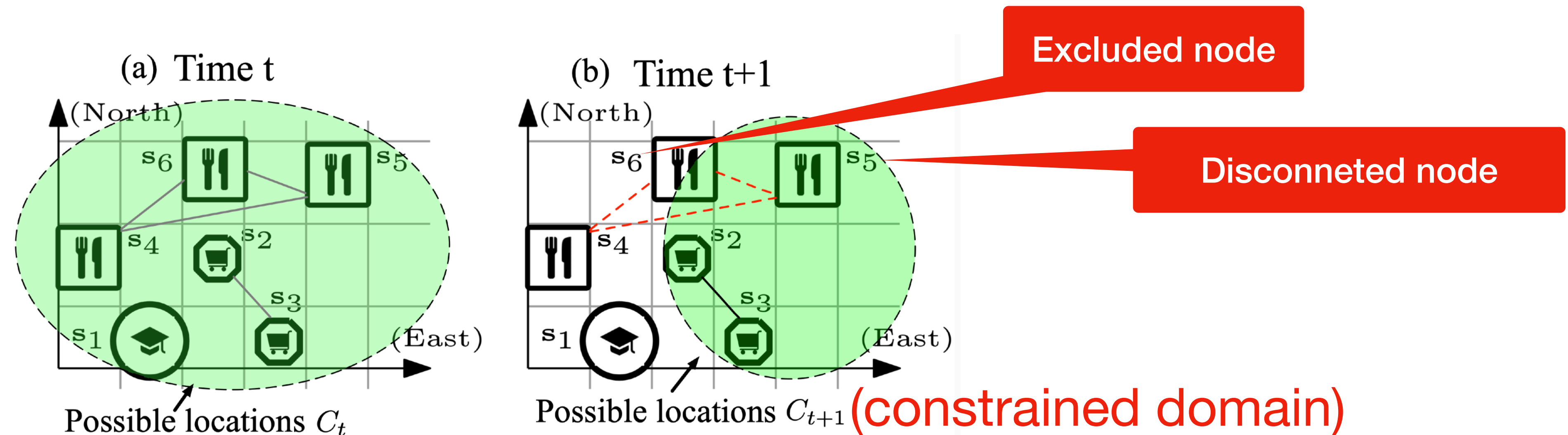
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PGLP for Continuous Release

Challenges

- The user possible location set may change over time.



- Location Exposure** under constrained domain:
If the user is at s_5 , the attacker may be able to figure out her true loc.
- Not all of the disconnected node will lead to Location Exposure, which also depends on the mechanism.

PGLP for Continuous Release

Countermeasure: Risk Detection and Policy Repair algorithm

- Detect Isolated Node in a policy graph

Isolated Node: the disconnected node that causes location exposure.

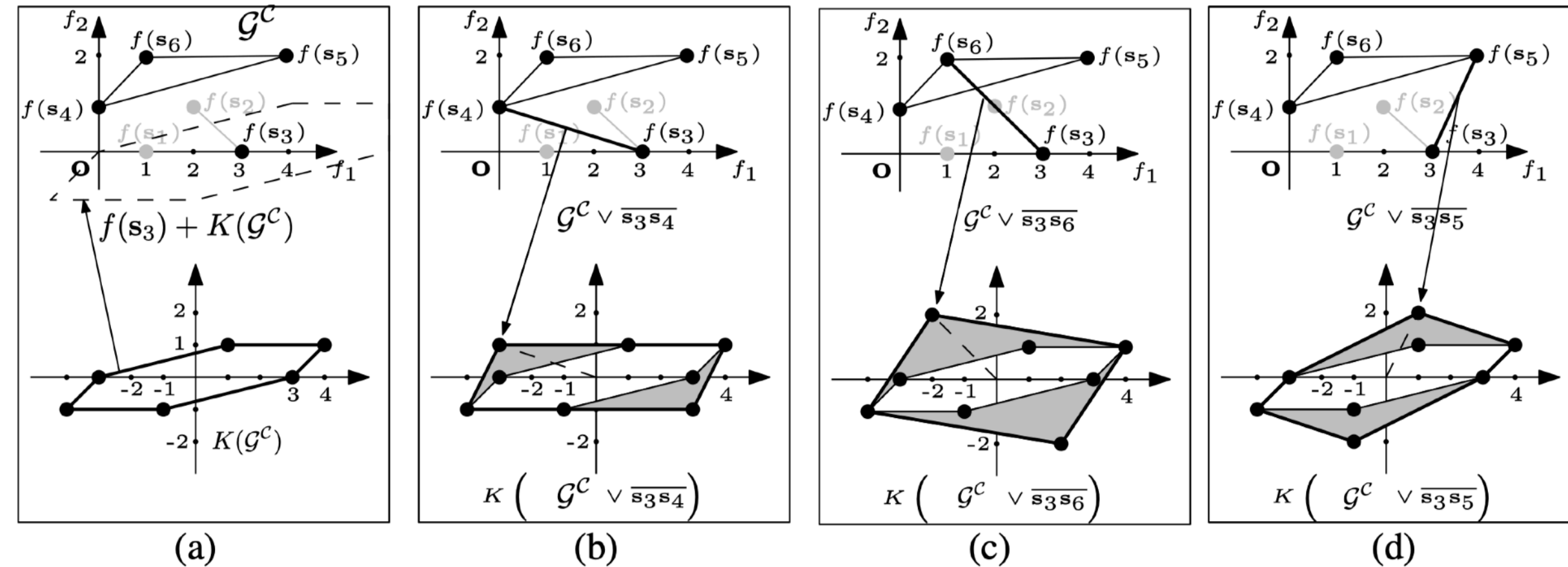
- Repair a policy graph with high utility.

Key idea: add an edge to protect the isolated node.

Algorithm 3 Finding Isolated Node

Require: \mathcal{G} , \mathcal{C} , disconnected node $\mathbf{s}_i \in \mathcal{C}$.

- 1: $\Delta f^{\mathcal{G}} = \bigvee_{\overline{\mathbf{s}_j \mathbf{s}_k} \in \mathcal{E}^{\mathcal{C}}} (f(\mathbf{s}_j) - f(\mathbf{s}_k));$
 - 2: $K(\mathcal{G}^{\mathcal{C}}) \leftarrow \text{Conv}(\Delta f^{\mathcal{G}});$
 - 3: **for all** $\mathbf{s}_j \in \mathcal{C}, \mathbf{s}_j \neq \mathbf{s}_i$ **do**
 - 4: **if** $\text{Conv}(\Delta f^{\mathcal{G}}, f(\mathbf{s}_j) - f(\mathbf{s}_i)) == K(\mathcal{G}^{\mathcal{C}})$ **then**
 - 5: **return false**
 - 6: **end if**
 - 7: **end for**
 - 8: **return true**
-



See our paper for more details.

PGLP for Continuous Release

An end-to-end Location Trace release framework

- Pipelines the *calculation of constrained domains, isolated node detection, policy graph repair, and private location release mechanism.*
- Utilizing HMM model (assume transition and initial probabilities are known)

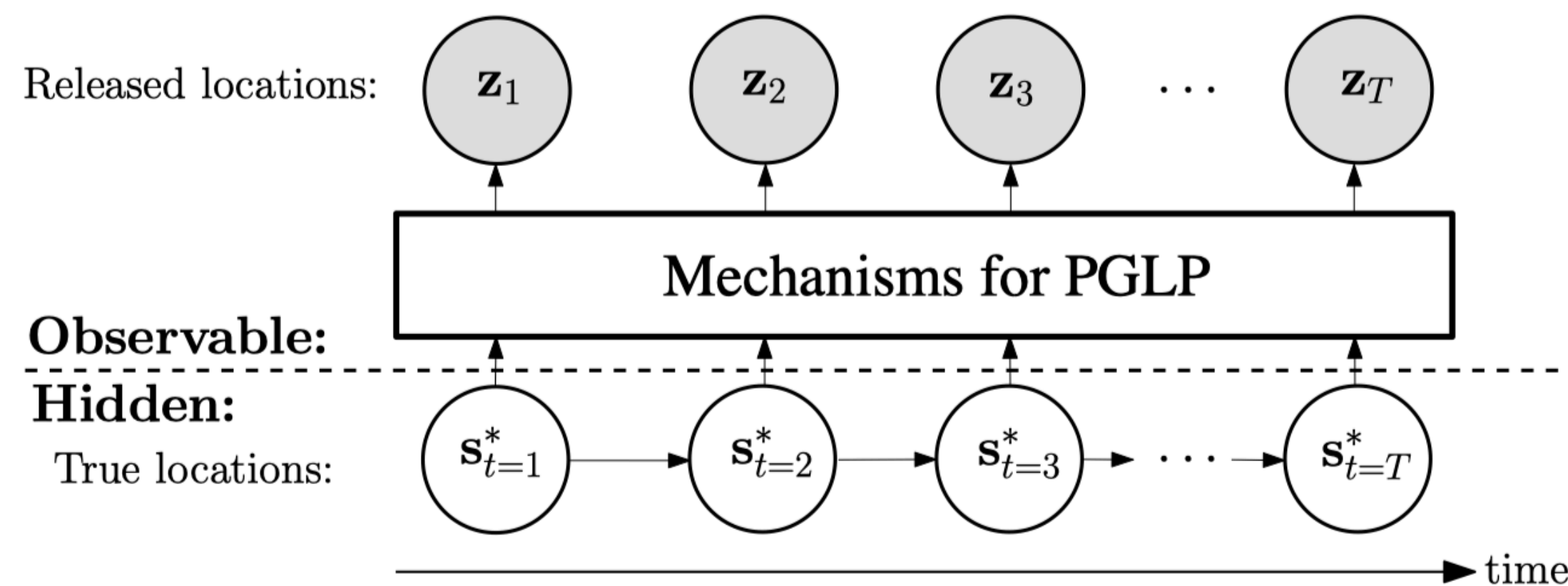


Fig. 5: Private location trace release via HMM.

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Experiments

- How different location policy graphs affect the privacy-utility tradeoffs?

- Settings:

- Two types of location policy graphs:

- “block-graph”: G_{k9}, G_{k16}, G_{k25} suitable for weather apps

- “category-graph”: G_{poi} suitable for location-based advertising

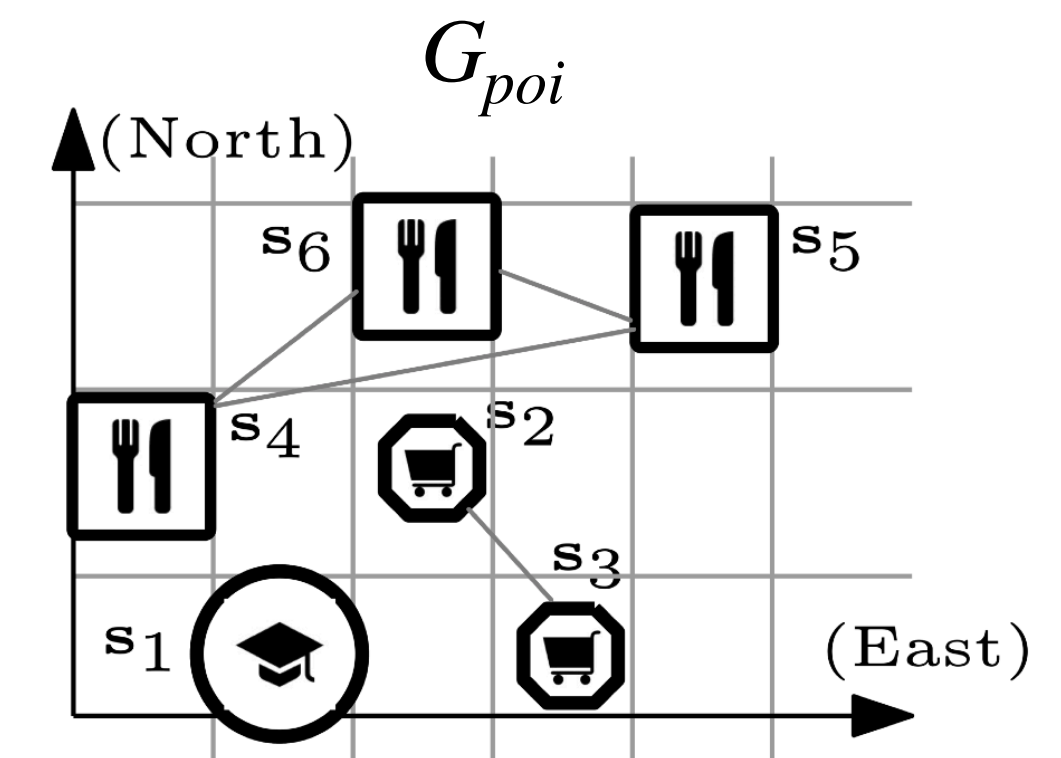
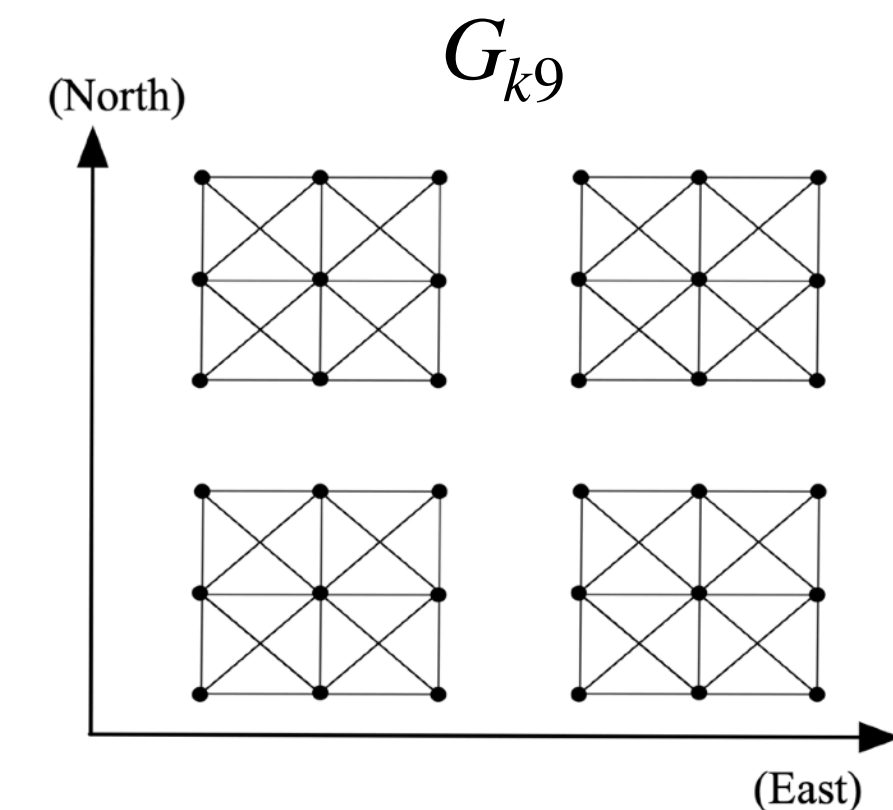
- Three types of Utilities

- E_{eu} : Euclidean distance between noisy and true locations.

suitable for weather apps

- E_r : L0 distance between **range queries** on noisy and true locations, like “whether the released location is in the same region with the true location”

- E_{poi} : L0 distance between **category queries** on noisy and true locations, like “whether the released location is the same category with the true location”.

suitable for location-based advertising

Experiments

E_{eu} , E_r , E_{poi} the lower the better.

Verified that we can flexibly design suitable policy w.r.t. the desired utility & privacy.

- Observations: G_{k9} is best for E_{eu} and E_r ; G_{poi} is the best for E_{poi} .

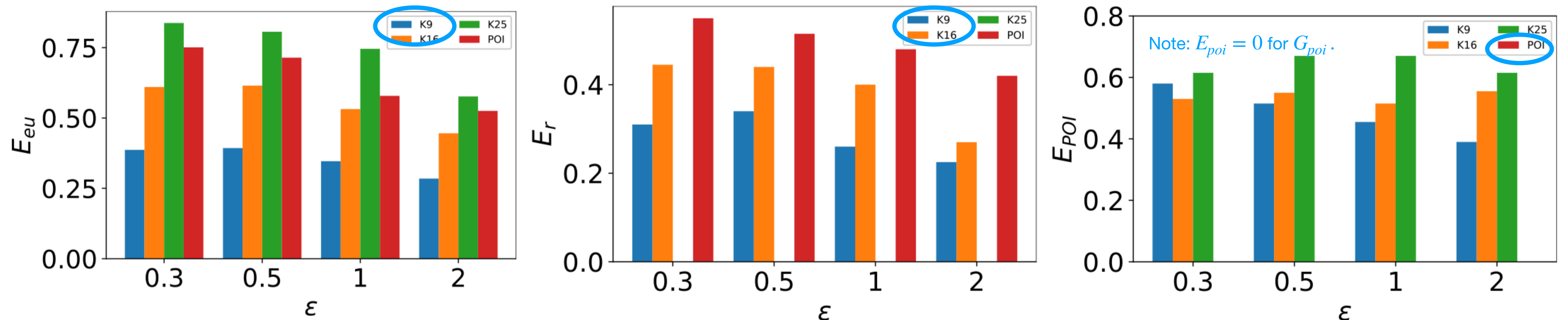


Fig. 7: Utility of different policy graphs.

(check the paper for more experimental results)

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Conclusion & Future Work

- Takeaway
 - PGLP provides a rich interface for privacy-utility tradeoff in location privacy.
- Future directions
 - Design advanced mechanisms for PGLP
 - Design optimal policy graphs for location-based applications, such as spatial crowdsourcing.